

## Final Exam Formula Sheet 17/18

### Chapter 10

$$\begin{aligned} \sin 2\alpha &= 2 \sin \alpha \cos \alpha, \\ \cos 2\alpha &= \cos^2 \alpha - \sin^2 \alpha = 1 - 2\sin^2 \alpha = 2 \cos^2 \alpha - 1 \\ \tan 2\alpha &= \frac{2 \tan \alpha}{1 - \tan^2 \alpha} \\ \sin \frac{\alpha}{2} &= \pm \sqrt{\frac{1 - \cos \alpha}{2}} & \cos \frac{\alpha}{2} &= \pm \sqrt{\frac{1 + \cos \alpha}{2}} \\ \tan \frac{\alpha}{2} &= \pm \sqrt{\frac{1 - \cos \alpha}{1 + \cos \alpha}} = \frac{\sin \alpha}{1 + \cos \alpha} = \frac{1 - \cos \alpha}{\sin \alpha} \end{aligned}$$

### Chapter 11

$$\begin{aligned} x &= r \cos \theta, y = r \sin \theta \\ r &= \pm \sqrt{x^2 + y^2}, \quad \tan \theta = \frac{y}{x} \\ r \operatorname{cis} \theta &= r(\cos \theta + i \sin \theta) \\ \sqrt[n]{z} &= z^{\frac{1}{n}} = r^{\frac{1}{n}} \operatorname{cis} \left( \frac{\theta}{n} + \frac{k \cdot 360}{n} \right) \end{aligned}$$

### Chapter 14

$$A^{-1} = \frac{1}{|A|} \begin{bmatrix} d & -b \\ -c & a \end{bmatrix}$$

### Chapter 13

$$\begin{aligned} t_n &= t_1 + (n-1)d & \sum_{k=1}^n k &= \frac{n(n+1)}{2} \\ t_n &= t_1 r^{n-1} & \sum_{k=1}^n k^2 &= \frac{n(n+1)(2n+1)}{6} \\ S_n &= \frac{n(t_1 + t_n)}{2} & \sum_{k=1}^n k^3 &= \left[ \frac{n(n+1)}{2} \right]^2 \\ S_n &= \frac{t_1(1-r^n)}{1-r}, r \neq 1 \\ \text{If } |r| < 1, \text{ then } \lim_{x \rightarrow \infty} r^n &= 0 \\ \text{If } |r| < 1, \text{ then } S_n &= \frac{t_1}{1-r}, r \neq 1 \end{aligned}$$

### Chapter 12

$$\begin{aligned} a^2 &= b^2 + c^2 - 2bc \cos A \\ b^2 &= a^2 + c^2 - 2ac \cos B \\ c^2 &= a^2 + b^2 - 2ab \cos C \end{aligned}$$

$$\begin{aligned} \mu &= \frac{v}{|v|} \\ \cos \theta &= \frac{u \cdot v}{|u||v|}, \quad \sin \theta = \frac{|u \times v|}{|u||v|} \end{aligned}$$

$$\begin{vmatrix} + & - & + \\ - & + & - \\ + & - & + \end{vmatrix}$$

$$\text{Area of a Parallelogram} = \begin{vmatrix} a_1 & b_1 \\ a_2 & b_2 \end{vmatrix}$$

$$\text{Volume of a Parallelepiped} = \begin{vmatrix} a_1 & b_1 & c_1 \\ a_2 & b_2 & c_2 \\ a_3 & b_3 & c_3 \end{vmatrix}$$

### Chapter 15

$$\begin{aligned} n(A \cup B) &= n(A) + n(B) - n(A \cap B) \\ n(A) &= n(U) - n(\bar{A}) \\ nC_r &= \frac{n!}{(n-r)!r!}, \quad nP_r = \frac{n!}{(n-r)!} \\ (a+b)^n &= {}_nC_0 a^n b^0 + {}_nC_1 a^{n-1} b^1 + {}_nC_2 a^{n-2} b^2 + \dots + {}_nC_n a^0 b^n \end{aligned}$$

### Chapter 16

$$\begin{aligned} P(B|A) &= \frac{P(A \cap B)}{P(A)} \\ [p + (1-p)]^n &= {}_nC_n p^n + \dots + {}_nC_k p^k (1-p)^{n-k} + \dots + {}_nC_0 (1-p)^n \end{aligned}$$

### Chapter 19

A function is continuous at  $x = c$   
If  $\lim_{x \rightarrow c} f(x) = f(c)$

### Chapter 17

$$\begin{aligned} \sigma &= \sqrt{\sigma^2} = \sqrt{\frac{(x_1 - \bar{x})^2 + (x_2 - \bar{x})^2 + \dots + (x_n - \bar{x})^2}{n}} \\ z &= \frac{x - \bar{x}}{\sigma} \end{aligned}$$

$$\begin{aligned} \hat{p} - 2 \sqrt{\frac{\hat{p}(1-\hat{p})}{n}} < p < \hat{p} + 2 \sqrt{\frac{\hat{p}(1-\hat{p})}{n}} \\ \hat{p} - 3 \sqrt{\frac{\hat{p}(1-\hat{p})}{n}} < p < \hat{p} + 3 \sqrt{\frac{\hat{p}(1-\hat{p})}{n}} \end{aligned}$$

z	.0	.1	.2	.3	.4	.5	.6	.7	.8	.9
-3	.0013	.0010	.0007	.0005	.0003	.0002	.0002	.0001	.0001	.0000+
-2	.0228	.0179	.0139	.0107	.0082	.0062	.0047	.0035	.0026	.0019
-1	.1587	.1357	.1151	.0968	.0808	.0668	.0548	.0446	.0359	.0287
-0	.5000	.4602	.4207	.3821	.3446	.3085	.2743	.2420	.2119	.1841
0	.5000	.5398	.5793	.6179	.6554	.6915	.7257	.7580	.7881	.8159
1	.8413	.8643	.8849	.9032	.9192	.9332	.9452	.9554	.9641	.9713
2	.9772	.9821	.9861	.9893	.9918	.9938	.9953	.9965	.9974	.9981
3	.9987	.9990	.9993	.9995	.9997	.9998	.9998	.9999	.9999	1.0000-