

**Chapter 5 Part 1 Test Review (Attn: This review DOES NOT include Section 5.6)**

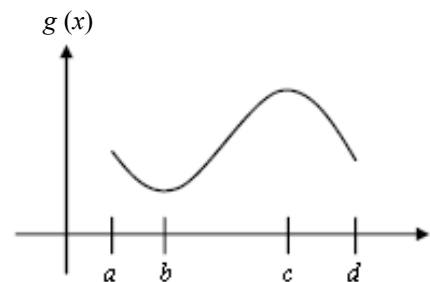
1. When looking for absolute extrema, where do the possible extrema exist, and how do you find them?
2. How do you justify relative extrema?
3. How do you justify that a function is increasing or decreasing?
4. How do you justify that a function is concave up or concave down?
5. How do you justify that a function has a point of inflection?
6. Using the graph of  $g(x)$  below, determine the signs of  $g'(x)$  and  $g''(x)$  at each point. Explain your reasoning.

At  $x = a$  ...

At  $x = b$  ...

At  $x = c$  ...

At  $x = d$  ...



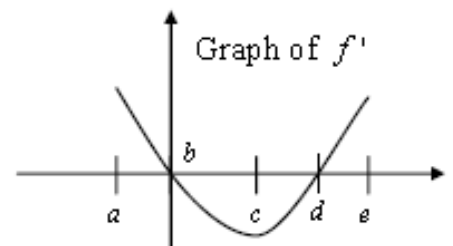
7. Given the graph of  $f'$  below answer each of the following questions, and justify your response with a statement that contains the phrase “since  $f'$  \_\_\_\_\_ ...”

a) When is  $f$  increasing?

b) When is  $f$  decreasing?

c) When is  $f$  concave up?

d) When is  $f$  concave down?



e) When does  $f$  have a relative maximum?

f) When does  $f$  have a relative minimum?

g) When does  $f$  have a point of inflection?

8. Find the value of  $c$  guaranteed by the MVT for  $f(x) = 4x^2 + 5x$  on the interval  $[-2, 1]$ .

9. [Calculator Allowed] Find the value of  $c$  guaranteed by the MVT for  $f(x) = \sin x$  on the interval  $[4, 5]$ .

[🎸: For those of you doing this problem algebraically, the answer is NOT  $c \approx 1.774 \dots$  Why?]

10. Suppose  $y = x^3 - 3x$ . [No Calculator]

a) Find the zeros of the function.

b) Determine where  $y$  is increasing or decreasing and justify your response.

c) Determine all local extrema and justify your response.

d) Determine the points where  $y$  is concave up or concave down, and find any points of inflection. Justify your responses.

e) Use all your information to sketch a graph of this function.

12. If  $f'(x) = x^2 - 9x + 1$ , what does  $f(x)$  equal?

13. Suppose  $\frac{d^2y}{dx^2} = x^3 - 4x^2$ . Justify each response below.

a) Where is  $y$  concave up?

b) Where is  $y$  concave down?

c) Are there any inflection points on  $y$ ? If so, where?

14. [Calculator Allowed] The derivative of  $h(x)$  is given by  $h'(x) = 2 \cos(x - \frac{\pi}{6}) + 1$  on the interval  $[-2\pi, 2\pi]$ . Justify EVERY response.

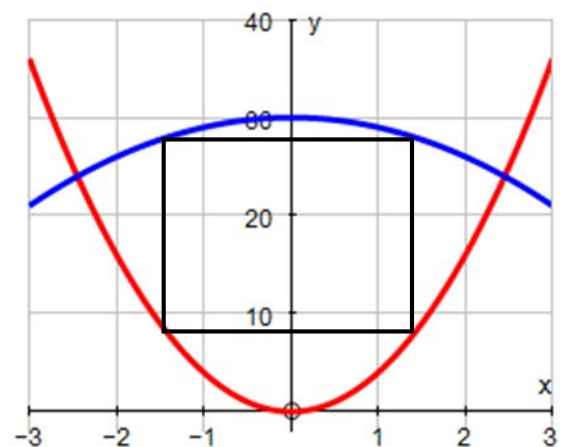
a) Where is  $h(x)$  increasing?

b) Where is  $h(x)$  concave down?

c) Find the  $x$ -coordinates of all extrema of  $h(x)$  on the interval  $[-2\pi, 2\pi]$ .

d) Does  $h(x)$  have a point(s) of inflection? If so, where?

15. A rectangle is inscribed between the parabolas  $y = 4x^2$  and  $y = 30 - x^2$  as shown in the picture. What is the maximum area of such a rectangle? Justify your response using CALCULUS.



16. **USE CALCULUS:** Find the maximum area of a rectangle inscribed under the curve  $f(x) = \sqrt{16 - x^2}$ .

17. [Calculator Allowed] **USE CALCULUS:** A rectangle is inscribed under one arch of  $y = 8 \cos(0.3x)$  with its base on the  $x$ -axis and its upper two vertices on the curve symmetric about the  $y$ -axis. What is the largest area the rectangle can have?

18. The function  $f$  is continuous on  $[0, 3]$  and satisfies the following:

$x$	0	$0 < x < 1$	1	$1 < x < 2$	2	$2 < x < 3$	3
$f$	0	Neg	-2	Neg	0	Pos	3
$f'$	-3	Neg	0	Pos	DNE	Pos	4
$f''$	0	Pos	1	Pos	DNE	Pos	0

a) Find the absolute extrema of  $f$  and where they occur.

b) Find any points of inflection.

c) Sketch a possible graph of  $f$ .